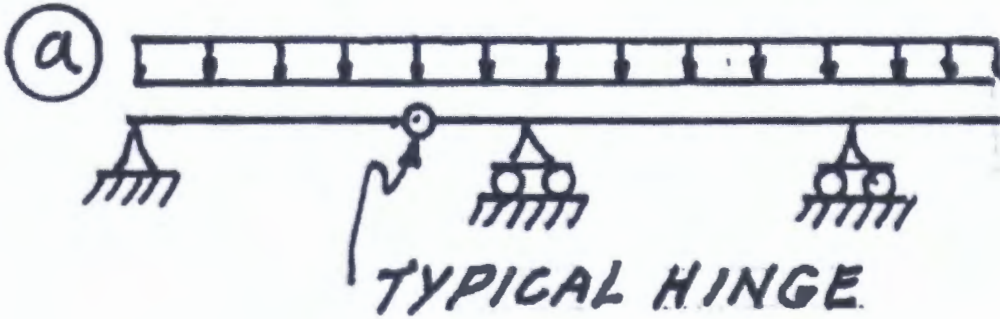


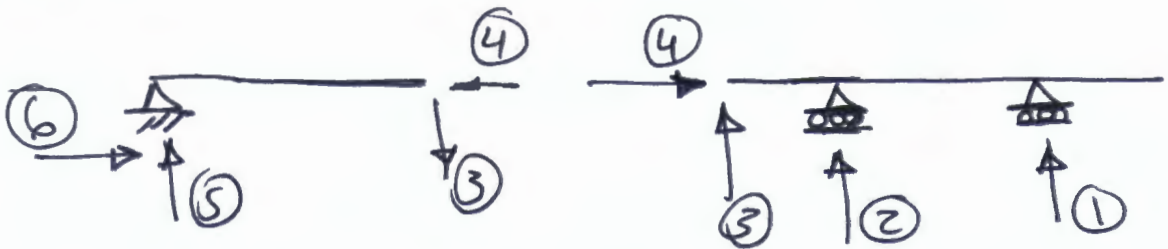
①

①

Q1a



$m =$  number of members in structure  
 $r =$  number of reactions



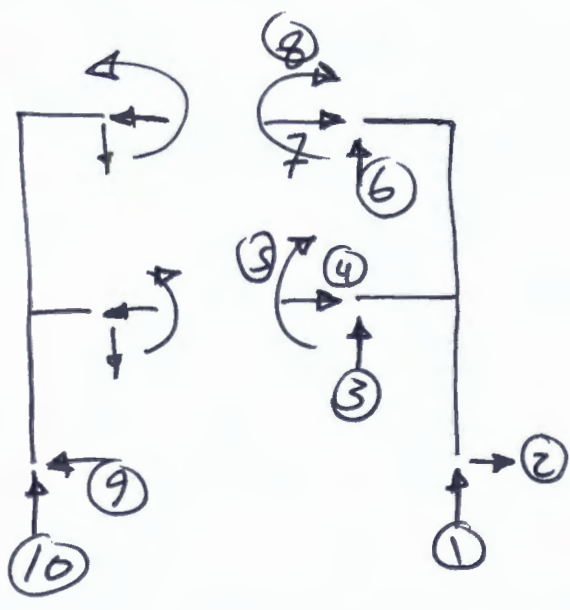
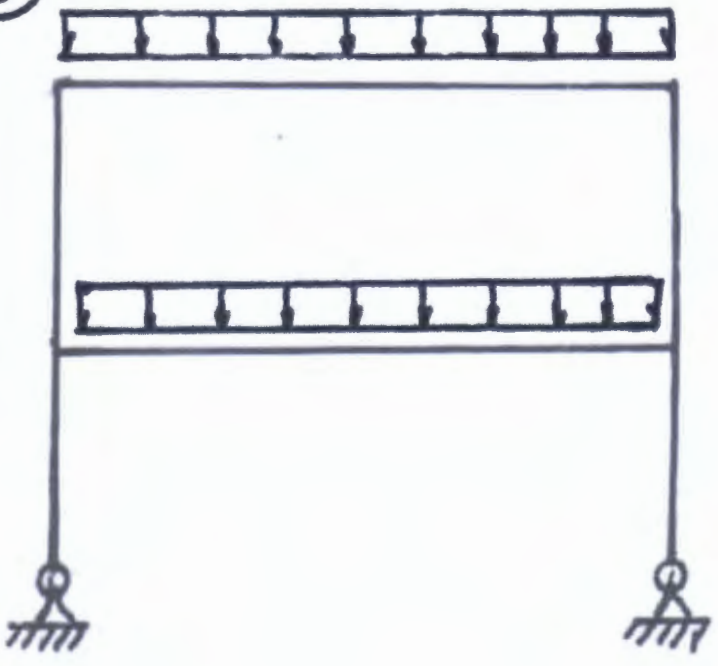
The structure is stable by inspection.

$$r = 6, \quad m = 2$$

$$\therefore r = 3m \quad \therefore \text{statically determinate}$$

Q1b

b



\* stable by inspection

$r = 10$  ,  $m = 2$

$3m = 6$   $\therefore r - 3m = 4$

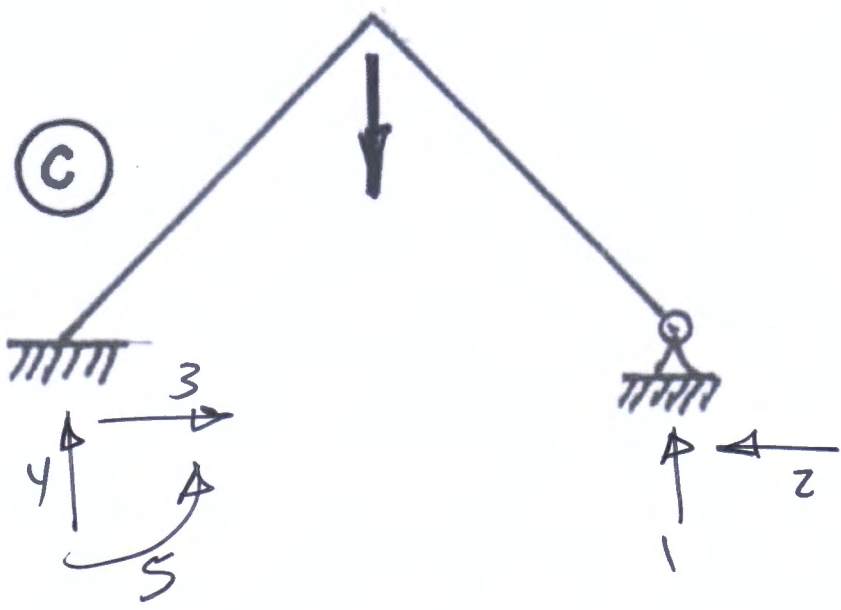
$\therefore$  Statically indeterminate to 4<sup>th</sup> degree

For special loading case stated  
 reactions ③ & ⑥ may be eliminated  
 to symmetry

Then for special loading it is  
 Statically indeterminate to 2<sup>nd</sup> degree



Q1c



Stable by inspection

$m = 1 \quad r = 5$

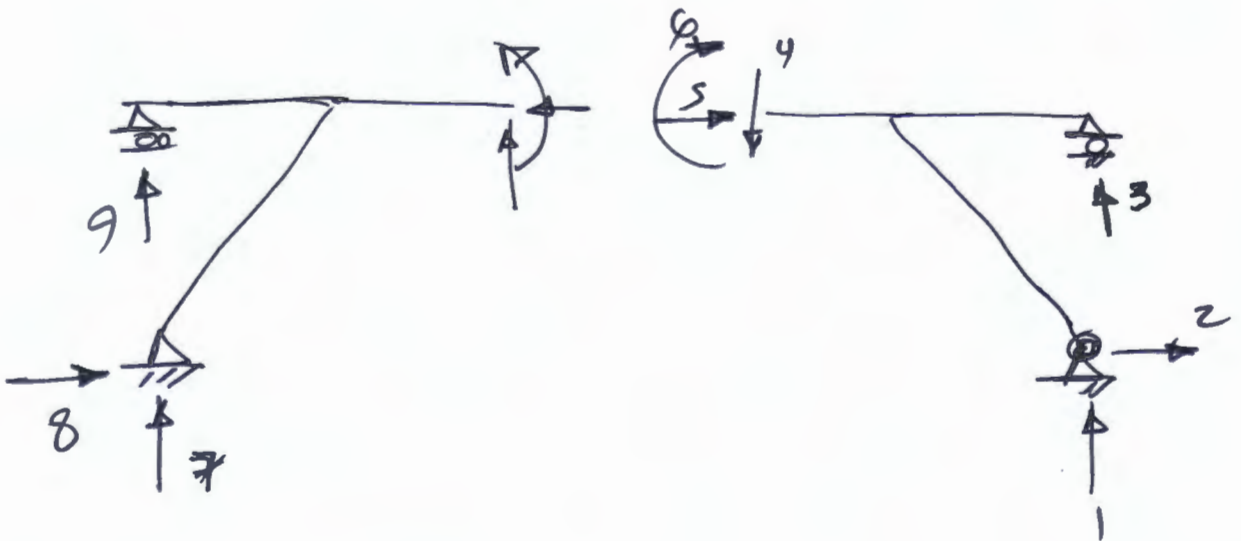
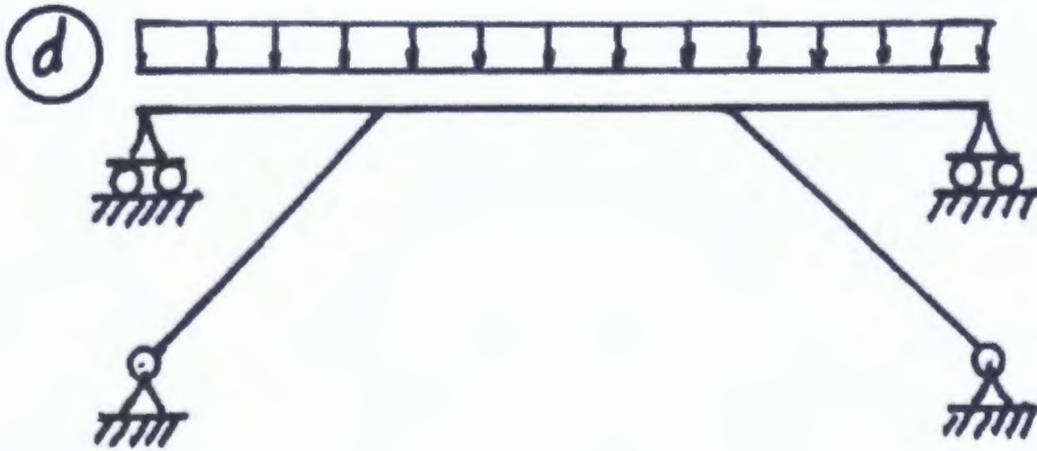
$r - 3m = 2$

∴ statically Indeterminate to the 2nd degree

Q1d

4

stable by inspection.



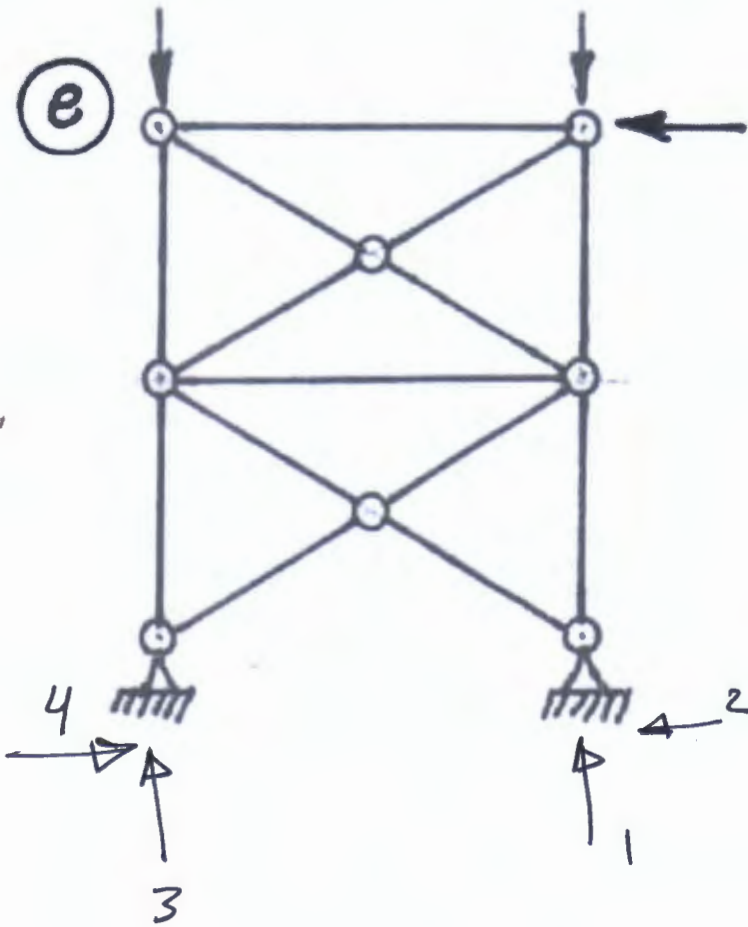
$$r = 9, \quad m = 2$$

$r - 3m = 3$   $\therefore$  statically indeterminate to 3<sup>rd</sup> degree

due to symmetry it becomes 2<sup>nd</sup> degree.

Q1e

5



Stable by inspection

$b$  = number of bars  
 $j$  = number of joints  
 $r$  = number of reactions

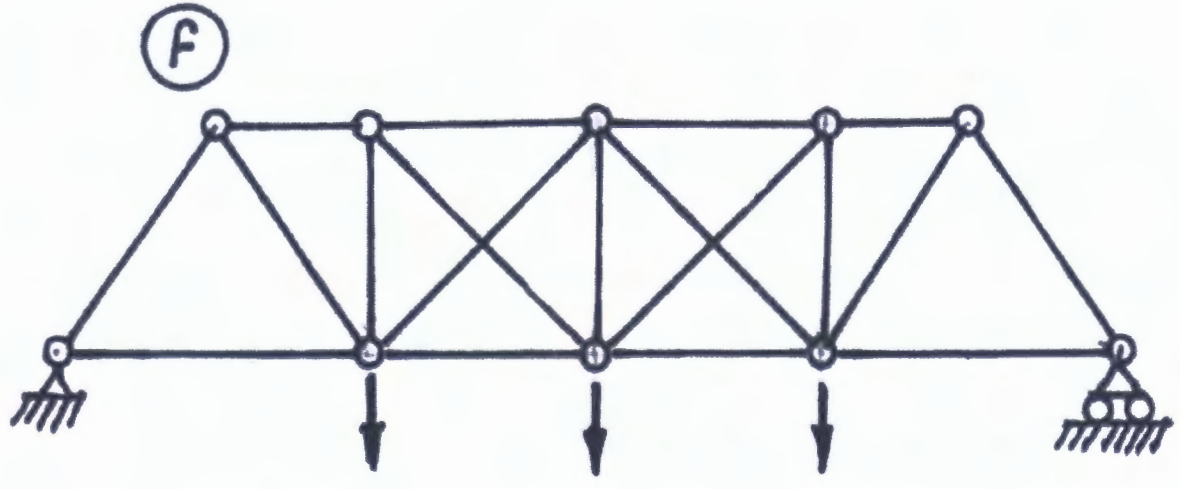
$$r = 4, \quad b = 14, \quad j = 8$$

$$b + r = 18$$

$$\therefore b + r > 2j$$

$\therefore$  statically indet.  
to 2<sup>nd</sup> degree

Q11



Stable by inspection

$$r = 3, b = 18, j = 10$$

$$b + r = 21 \rightarrow 2j = 20$$

∴ Statically indeterminate to the  $(21 - 20 = 1)$  1st degree



Q2a

(a)

$$\sum M_d = 0$$

$$R_1 = \frac{90 \times 6 + 72 \times 15}{12} = 135$$

$$\sum M_b = 0$$

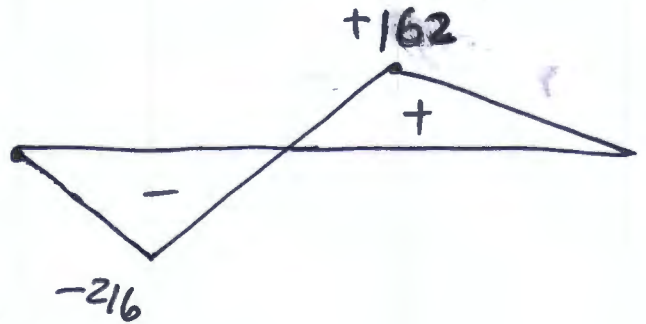
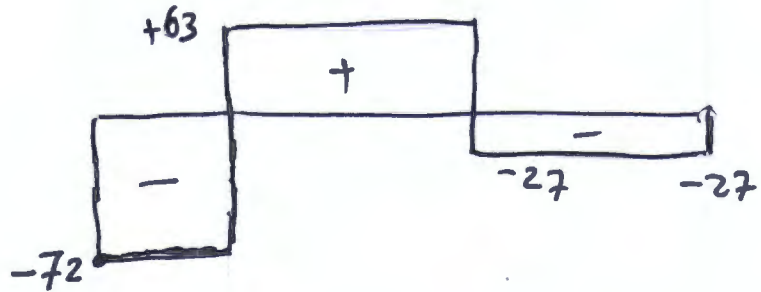
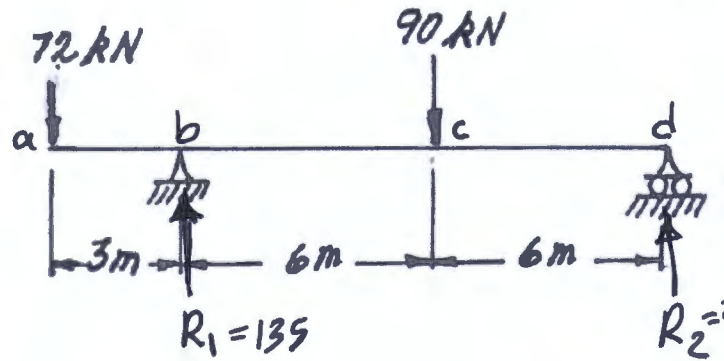
$$R_2 = \frac{90 \times 6 - 72 \times 3}{12} = 27 \text{ kN}$$

$$\text{Max. shear -} = -72 \text{ kN}$$

$$\text{Max. shear +} = +63 \text{ kN}$$

$$\text{Max. Moment +} = +162 \text{ kN.m}$$

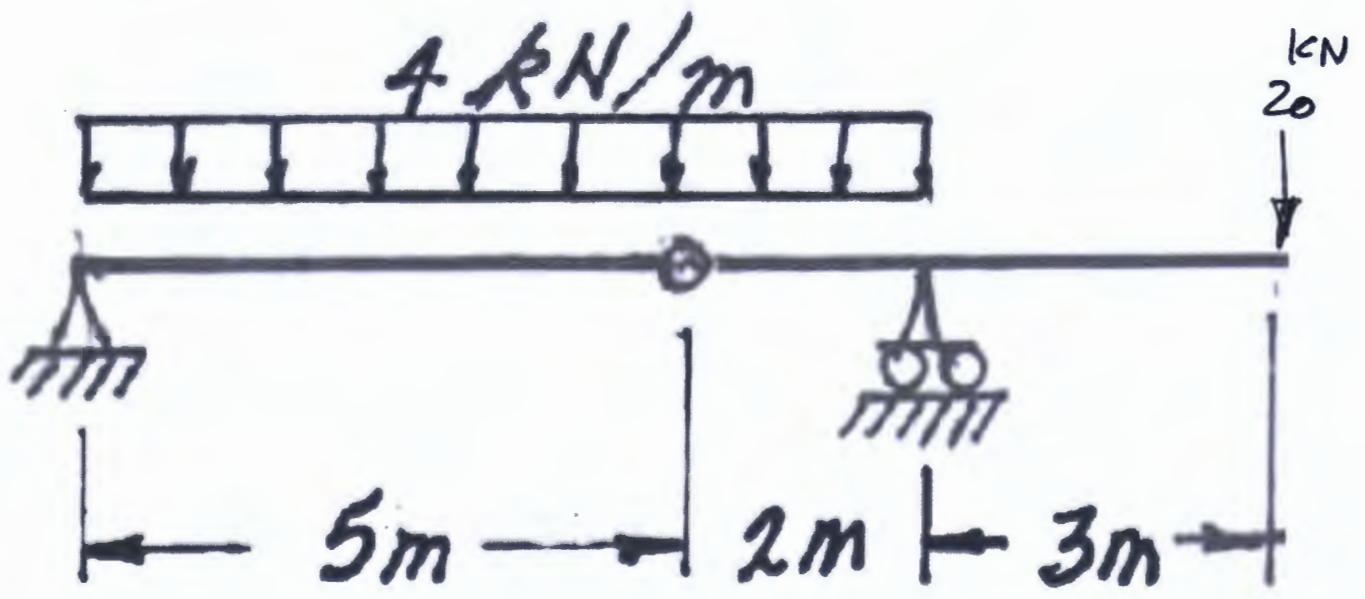
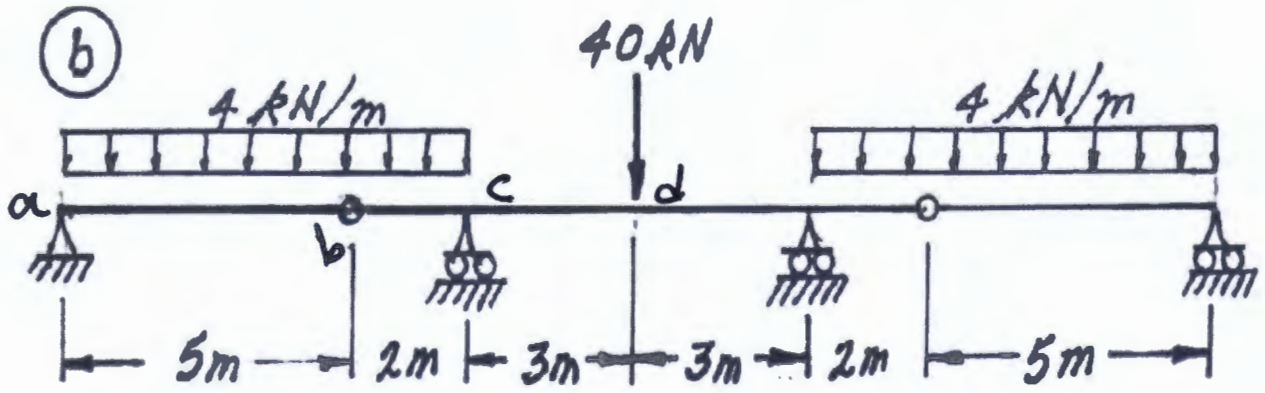
$$\text{Max. Moment -} = -216 \text{ kN.m}$$



==

Q2b

8



Q2b

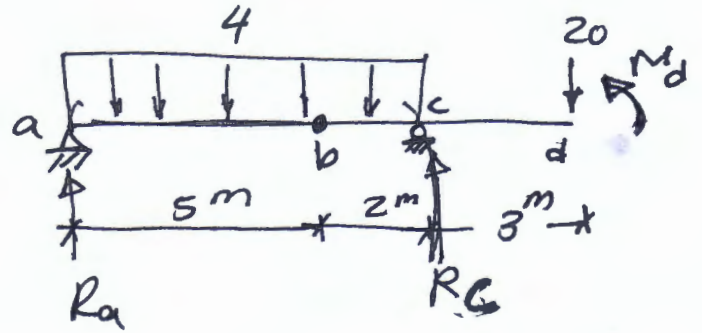
9

$$\sum M_a = 0$$

$$4 * \frac{7^2}{2} - M_d + 20(10)$$

$$- R_c * 7 = 0$$

$$\therefore 7R_c + M_d = 298 \quad \text{--- (1) ✓}$$



$$\sum M_c = 0$$

$$R_a * 7 - 4 * \frac{7^2}{2} + 20 * 3 - M_d = 0$$

$$\therefore 7R_a - M_d = +38 \quad \text{--- (2)}$$

$$\text{Eq (1) + Eq (2)} \Rightarrow 7(R_a + R_c) = 298 + 38$$

$$R_a + R_c = 48 \quad \text{--- (3)}$$

$$\sum M_b = 0$$

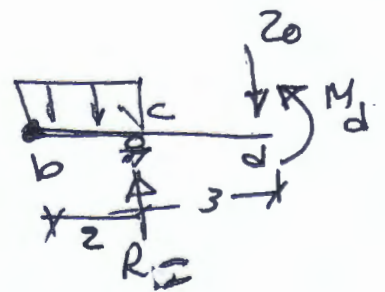
$$-R_c * 2 + 4 * \frac{2^2}{2} + 20 * 5 - M_d = 0$$

$$\therefore M_d + 2R_c = 108 \quad \text{--- (4)}$$

solve (1) & (4)  $\Rightarrow$

$$\text{Eq (1) - Eq (4)} \Rightarrow 5R_c = 298 - 108$$

$$R_c = 38 \text{ kN} \quad \text{--- } \uparrow$$



sub.  $R_c$  into (4)  $Q_2$

(10)

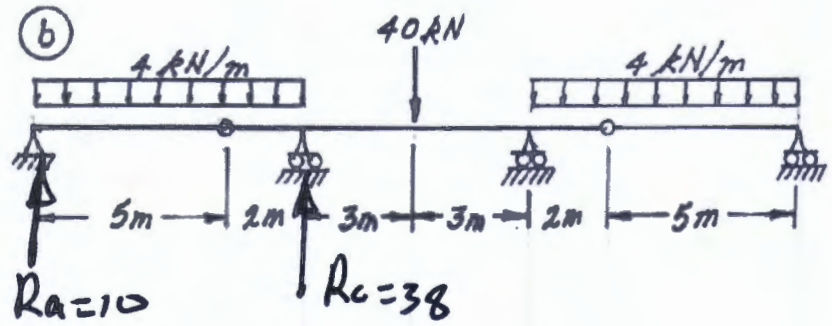
$$M_d + 2 \times 38 = 108 \Rightarrow M_d = +32 \text{ KN}\cdot\text{m}$$

sub.  $M_d$  in (2)

$$\Rightarrow 7R_a - 32 = 38 \Rightarrow R_a = 10 \text{ KN}$$

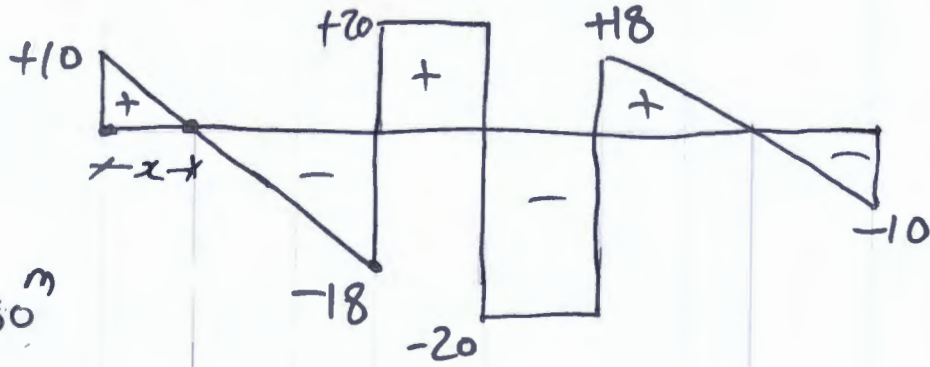
Q2b

(11)



Max. shear =  $+20 \text{ kN}$

Min. shear =  $-18 \text{ kN}$

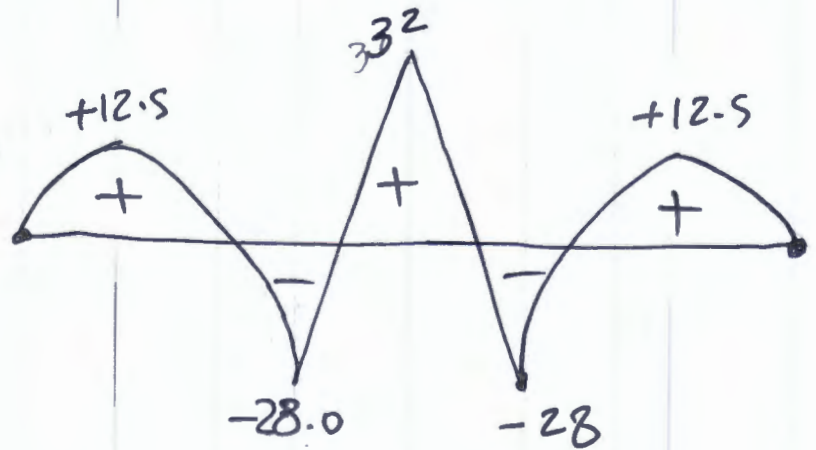


to find (x) for Max. Moment:

$$\frac{x}{10} = \frac{7}{28} \Rightarrow x = 2.50 \text{ m}$$

Max. Moment =  $+32 \text{ kN}\cdot\text{m}$

Min. Moment =  $-28 \text{ kN}\cdot\text{m}$



Q2c

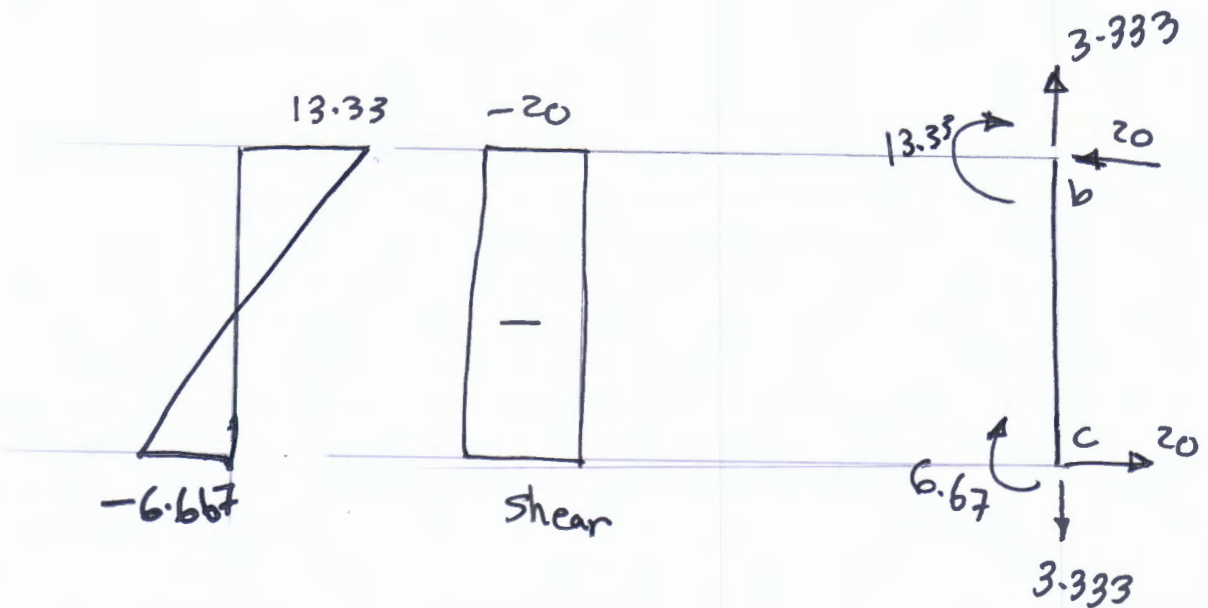
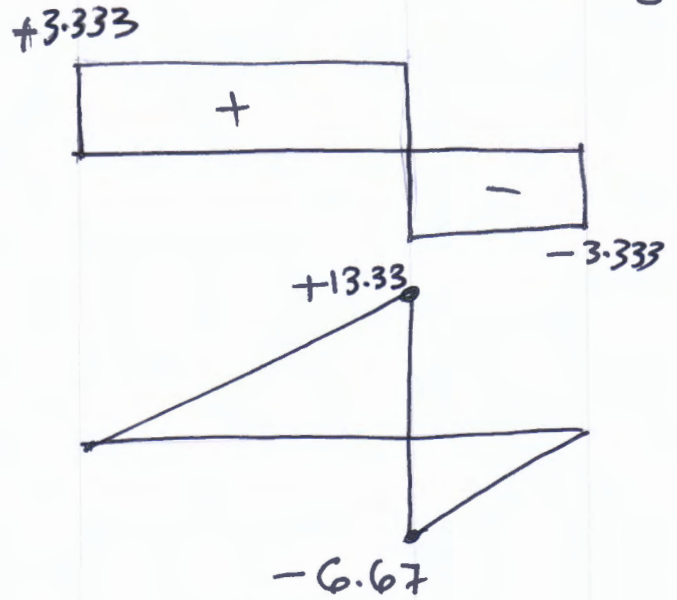
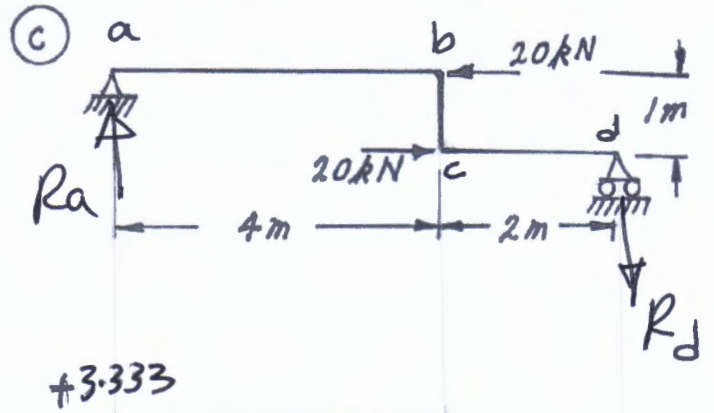
(12)

$$\sum M_d = 0$$

$$R_a * 6 - 20 * 1 = 0$$

$$R_a = 3.333 \text{ kN} \uparrow$$

$$R_d = 3.333 \text{ kN} \downarrow$$



So:

$$\text{Max. shear} = + 3.33 \text{ kN}$$

$$\text{Max. Moment} = 13.33$$

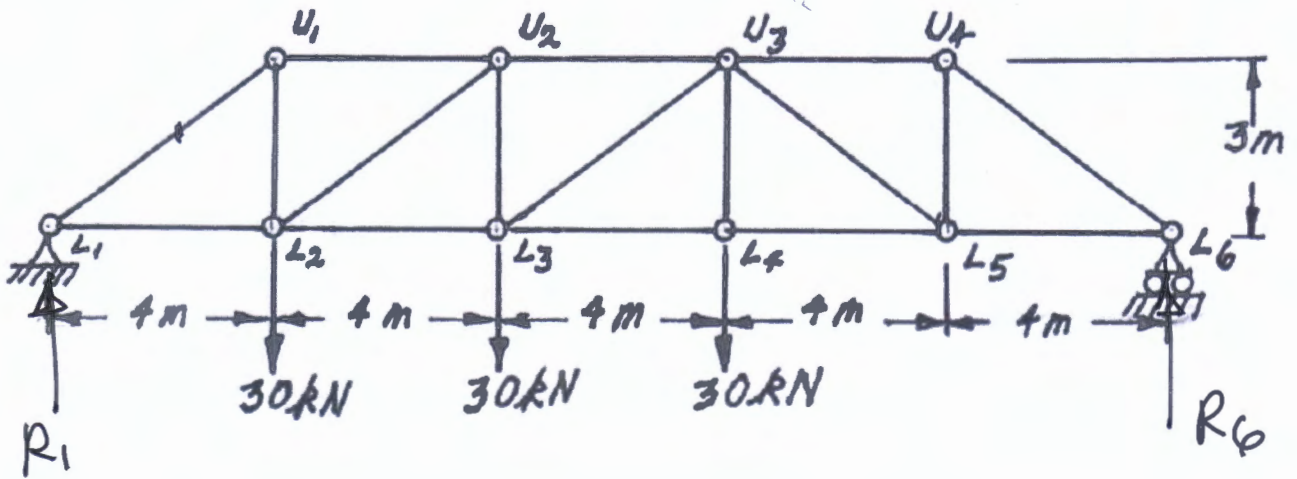
$$\text{Min. shear} = -20 \text{ kN}$$

$$\text{Min. shear} = -6.67 \text{ kN}$$

Q3

Q3

(13)



$$R_1 = \frac{30 \times 8 + 30 \times 12 + 30 \times 16}{20} = 54 \text{ kN}$$

$$R_6 = \frac{30 \times 4 + 30 \times 8 + 30 \times 12}{20} = 30$$

$$L_1 U_1 = \frac{5}{3} \times 54 = 90 \text{ kN comp.}$$

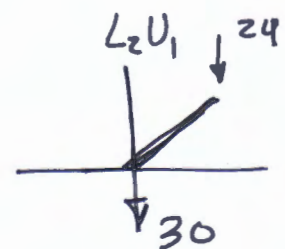
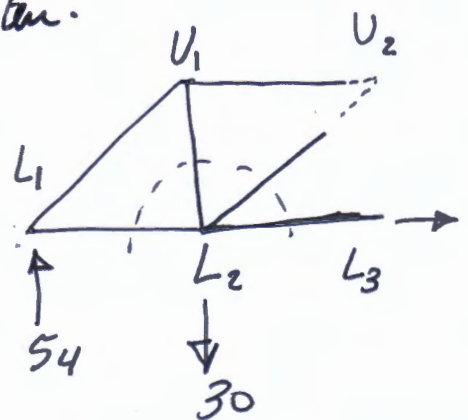
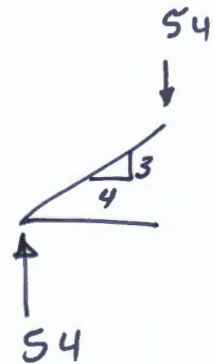
$$(L_2 L_3)(3) - 54 \times 8 = 0$$

$$L_2 L_3 = \frac{54 \times 8 - 30 \times 4}{3} = 104 \text{ kNm.}$$

$$L_2 U_2 = (54 - 30) \left(\frac{5}{3}\right)$$

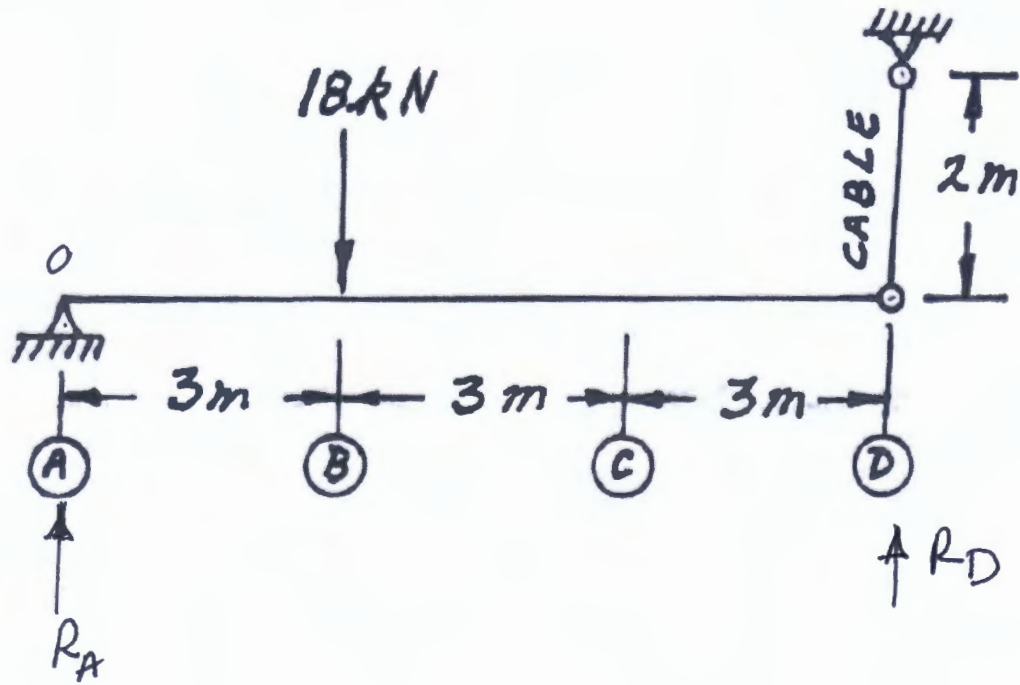
$$L_2 U_2 = 40 \text{ comp.}$$

$$L_2 U_1 = 24 + 30 = 54 \text{ tension.}$$



Q4

14



Solution:

a)  $R_D = \text{force in the cable} = \frac{18 \times 3}{9} = 6 \text{ kN}$

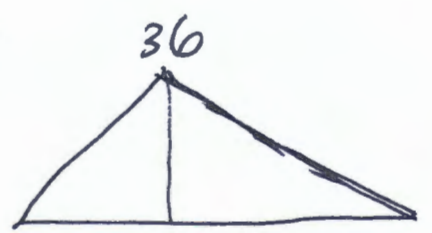
Elongation of cable =  $\frac{6 \times 2}{20000} = 0.0006 \text{ m}$

The beam will deflect due to beam elasticity and elongation of cable.

The deflection due to beam elasticity only will be computed by "Area-Moment" Method.

Bending Moment diagram:

Q4

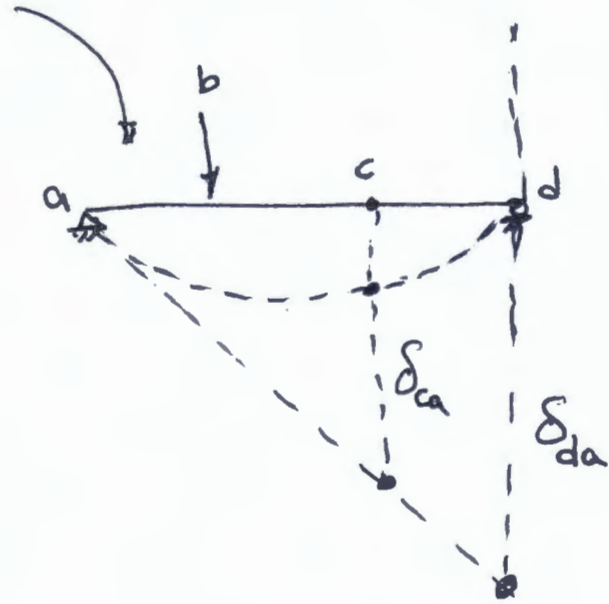


Refer to elastic curve below

$$\delta_{da} = \frac{1}{2} * 36 * 6 * \frac{2}{3} * 6 + \frac{1}{2} * 36 * 3 * (6 + \frac{1}{3} * 3)$$

$$\delta_{da} = 810/EI$$

$$\delta_{ca} = \frac{1}{2} * 36 * 3 * (3 * \frac{1}{3} * 3) + \frac{1}{2} * 18 * 3 * (\frac{2}{3} * 3) + 18 * 3 * 1.5 = 351/EI$$



$$\Delta_c = \frac{810}{EI} * \frac{2}{3} - \frac{351}{EI} + \frac{2}{3} * 0.006$$

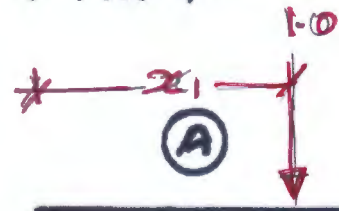
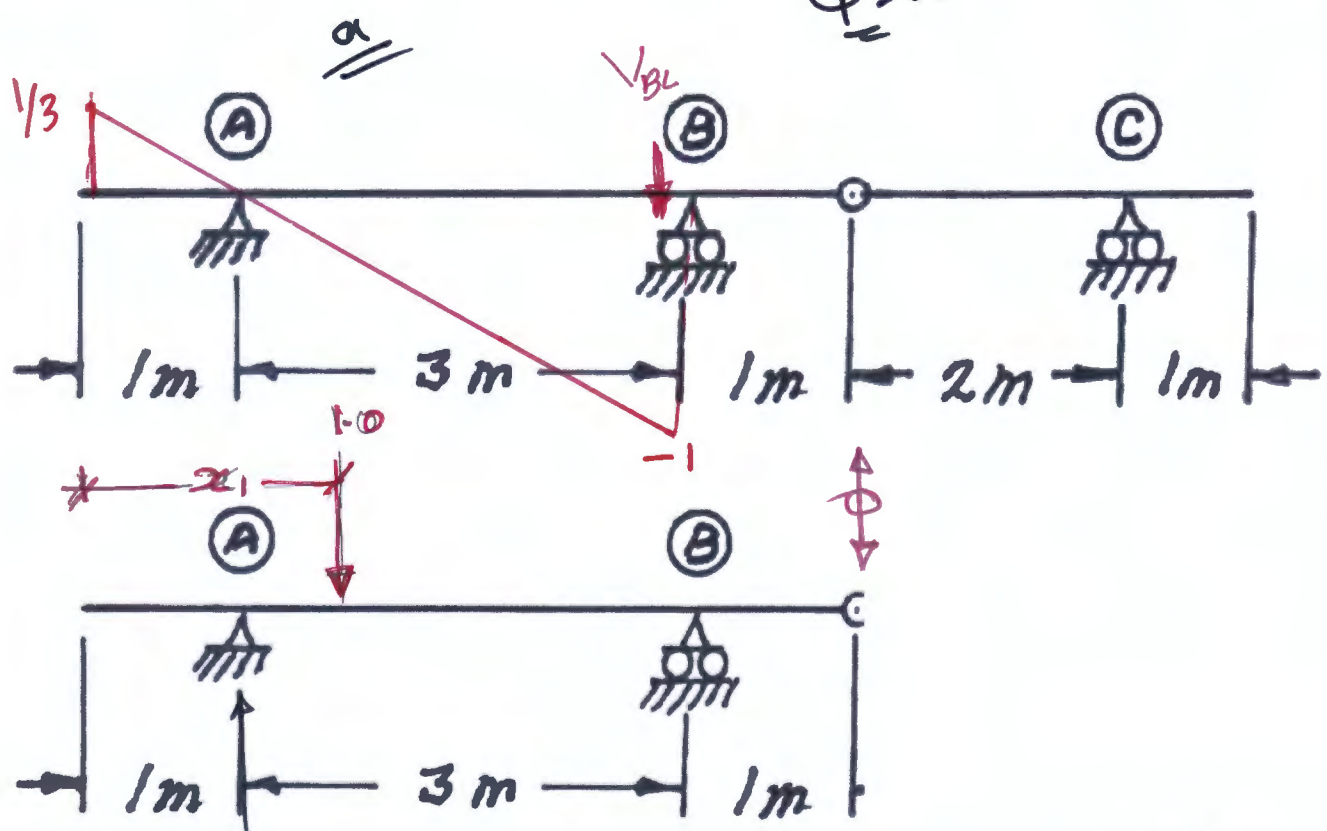
$$\Delta_c = \frac{189}{EI} + 0.004$$

$$\Delta_c = \frac{189}{21000} + 0.004 = 0.013 = 13 \text{ mm}$$

b)  $\Delta_b = \Delta_c$

This is attributed to Maxwell's theorem of Reciprocal displacements (Betti's Law)

Qsa



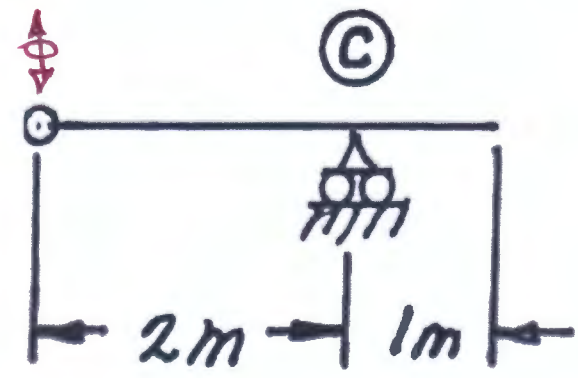
$0 \leq x_1 \leq 4$  (Region 1)

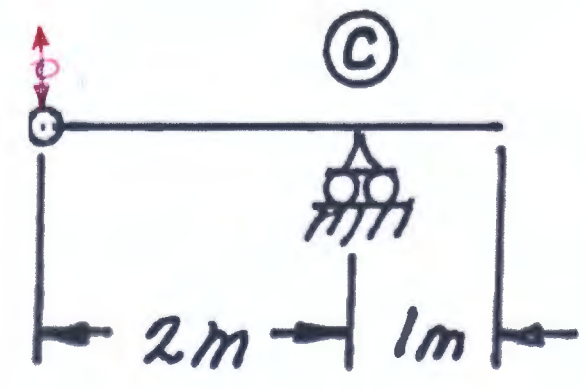
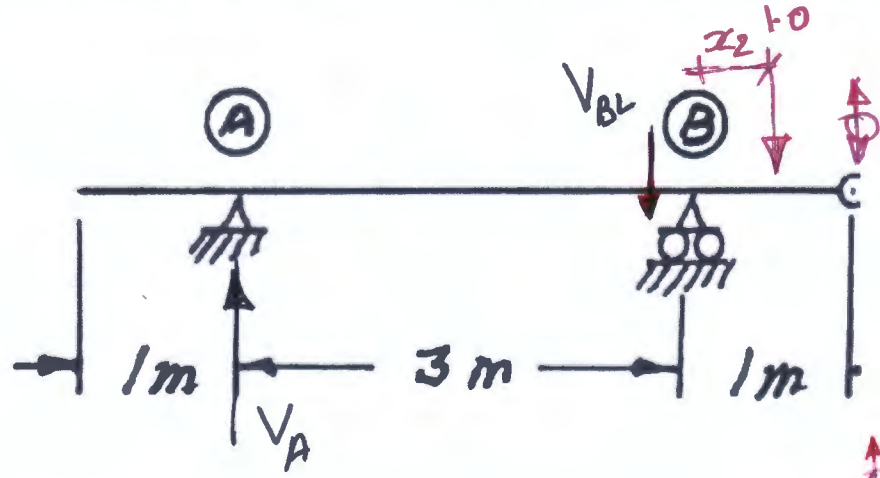
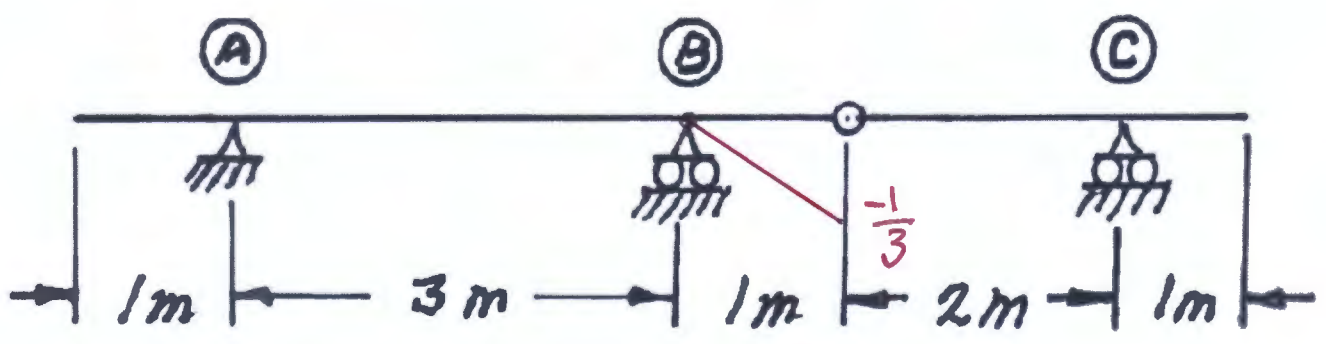
$$V_A = \frac{4 - x_1}{3}$$

$$V_A = \frac{4}{3} - \frac{x_1}{3}$$

$$\uparrow \sum F_y = 0 \quad V_{BL} + 1 = \frac{4}{3} - \frac{x_1}{3}$$

$$\therefore V_{BL} = \frac{1}{3} - \frac{x_1}{3}$$





Region ②

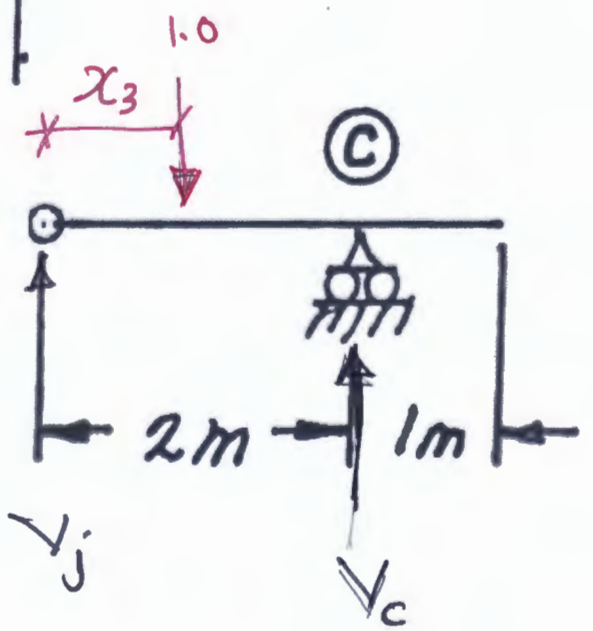
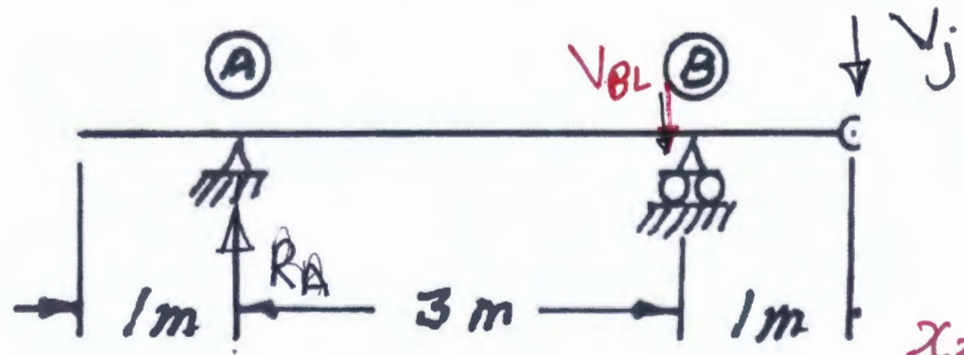
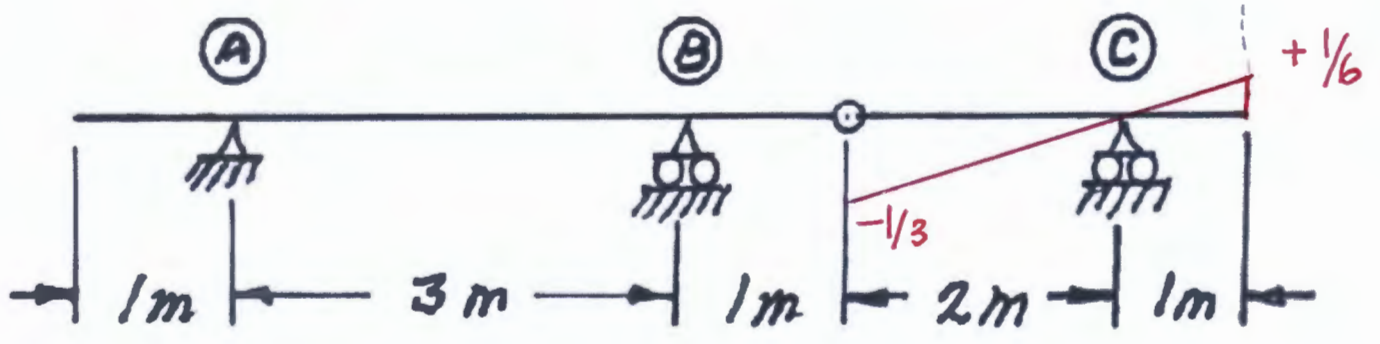
$$0 \leq x_2 \leq 1$$

$$V_A * 3 + 1 * x_2 = 0$$

$$V_A = -\frac{x_2}{3}$$

$$V_{BL} = V_A \Rightarrow V_{BL} = -\frac{x_2}{3}$$

Q5a



$0 \leq x \leq 3m$  Region ③

$$V_c * 2 = X_3$$

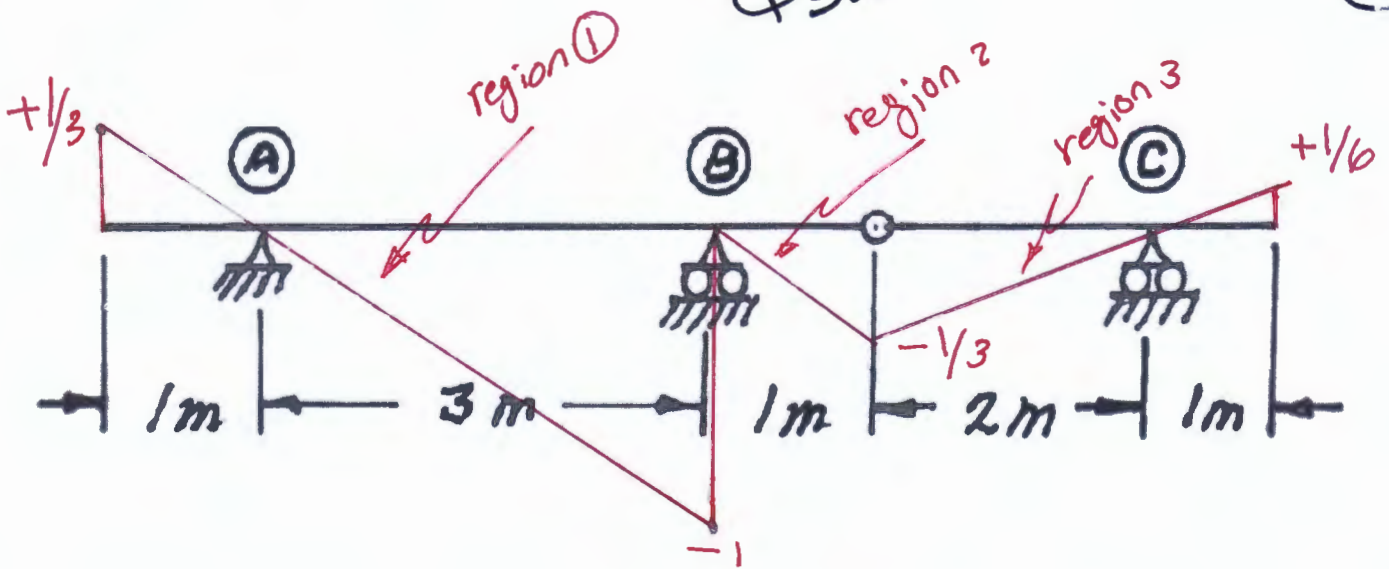
$$V_c = \frac{X_3}{2}$$

$$V_j = 1 - V_c$$

$$V_j = 1 - \frac{X_3}{2}$$

$$R_A * 3 + V_j * 1 = 0$$

$$V_{BL} = R_A = -\frac{V_j}{3} = \frac{-1}{3} + \frac{X_3}{6}$$



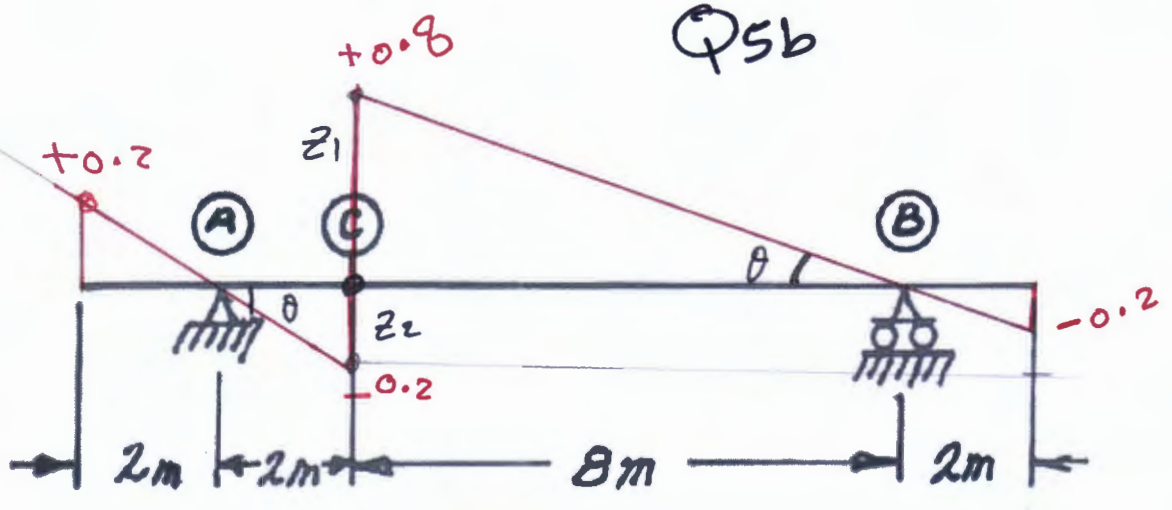
Complete Influence Line  
for the whole Structure

$$\text{Maximum + Value} = +\frac{1}{3}$$

$$\text{Maximum - Value} = -1$$

$$\text{Maximum absolute Value} = 1$$

Q5b



Shear @ C      Use Muller Breslau principle

We split @ C:  $z_1 + z_2 = 1$   $\begin{cases} z_1 = 8\theta \\ z_2 = 2\theta \end{cases}$   
 $\therefore 8\theta + 2\theta = 1 \quad \therefore \theta = 1/10$

$\therefore z_1 = 8\theta = 0.8, \quad z_2 = 2\theta = 0.2$

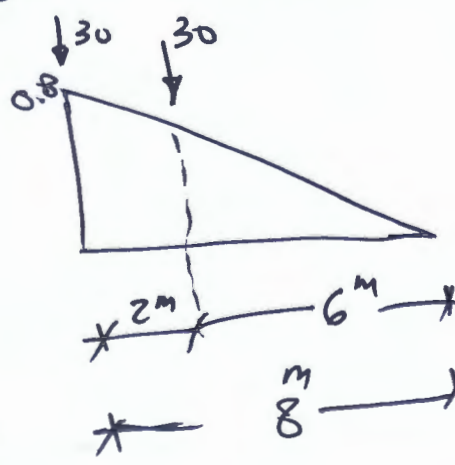
Max. Absolute shear:  
 Uniform Distributed Load:

$$6 \times 0.5 \times 0.8 \times 8 + 6 \times 0.5 \times 0.2 \times 2 = 20.4 \text{ kN}$$

Concentrated loads

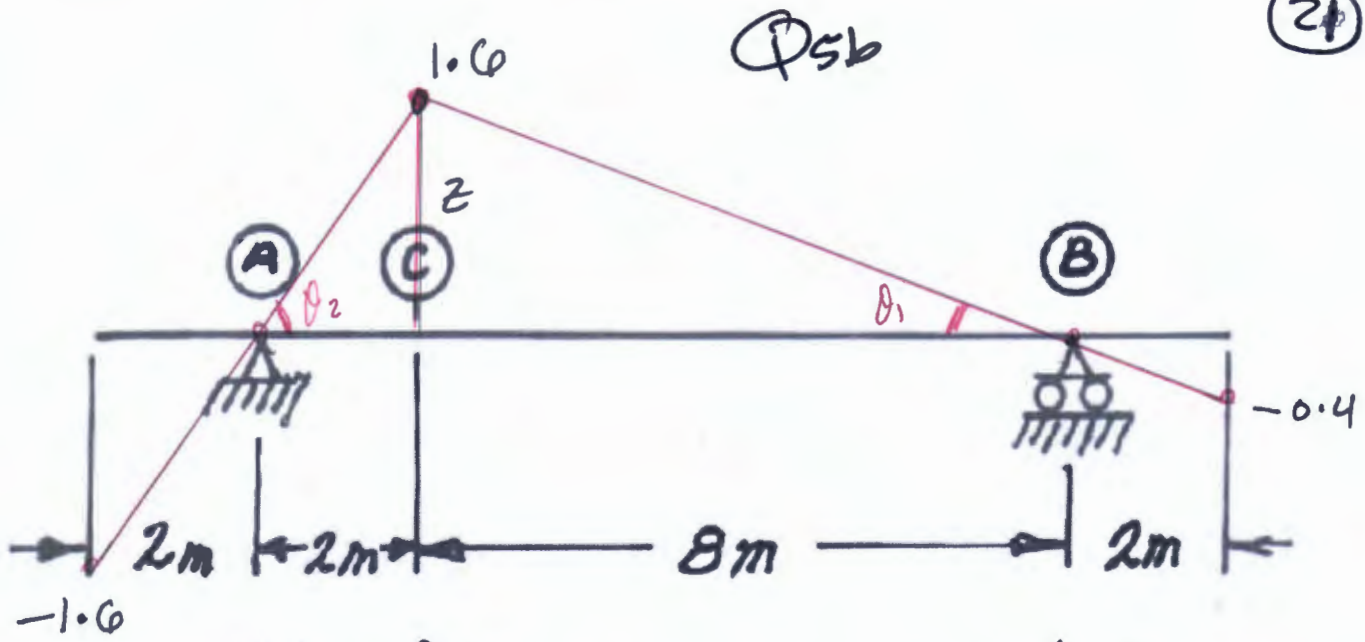
$$= 30 \times 0.8 + 30 \times \frac{6}{8} \times 0.8$$

$$= 42$$



Max. Absolute shear =  $20.4 + 42$   
 $= 62.4 \text{ kN}$

Q5b



Muller Breslau; Compute ordinate z:

$$\theta_1 + \theta_2 = 1 \Rightarrow \frac{z}{8} + \frac{z}{2} = 1$$

$$\therefore z + 4z = 8 \Rightarrow 5z = 8 \Rightarrow z = \frac{8}{5} = 1.6$$

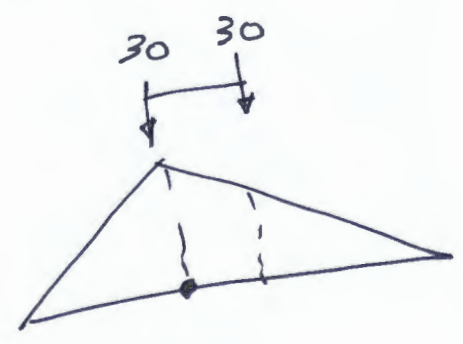
Max. Absolute Moment @ C:

UDL:  $6 * 0.5 * 1.6 + 10 = 48 \text{ KN}\cdot\text{m}$

Concentrated loads:

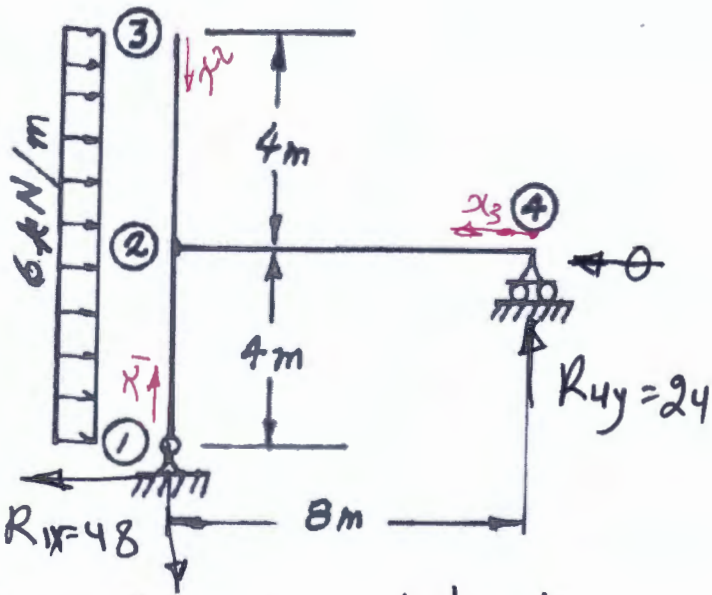
$$= 30 * 1.6 + 30 * \frac{6}{8} * 1.6$$

$$= 84 \text{ KN}$$



$\therefore$  Max. Absolute Moment @ C:

$$= 48 + 84 = 132 \text{ KN}\cdot\text{m}$$

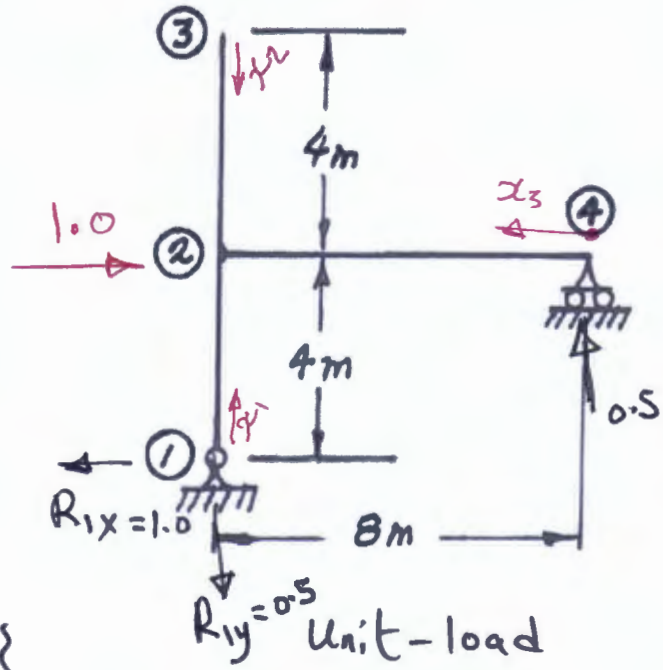


$R_{1y} = 24$  original loading

$$\sum F_x = 0 \Rightarrow R_{1x} = 6 \times 8 = 48 \text{ kN}$$

$$\sum M_4 = 0 \Rightarrow R_{1x} \times 4 - R_{1y} \times 8 = 0$$

$$\therefore R_{1y} = \frac{48 \times 4}{8} = 24 \text{ kN}$$



$R_{1y} = 0.5$  Unit-load

$$\sum F_x = 0 \Rightarrow R_{1x} = 1.0$$

$$R_{1y} \times 8 - R_{1x} \times 4 = 0$$

$$\therefore R_{1y} = 0.5 \text{ kN}$$

$$R_{4y} = 0.5 \text{ kN}$$

Deflection @  $z$ :  $\Delta_2$

$$\Delta_2 = \int_{\text{member 1-2}} + \int_{\text{member 2-3}} + \int_{\text{member 4-2}}$$

$$\int_{1-2} = \int_0^4 \frac{(48x_1 - 3x_1^2)(x_1)}{EI} dx_1 = \int_0^4 \frac{48x_1^2 - 3x_1^3}{EI} dx_1$$

$$\int_{1-2} = \frac{1}{EI} \left[ 16x_1^3 - \frac{3}{4}x_1^4 \right]_0^4 = 832/EI$$

$$\int_{2-3} = 0$$

Q8

$$\int_{4-2} = \int \frac{(24x_3)(0.5x_3)}{EI} dx_3 =$$

$$= \int \frac{12x_3^2}{EI} dx_3 = 4x_3^3 \Big|_0^8 = \frac{2048}{EI}$$

$$\therefore \Delta_2 = \frac{832}{EI} + 0 + \frac{2048}{EI} = \frac{2880}{EI}$$

$$\Delta_2 = \frac{2880}{1.8 \times 10^5} = \underline{\underline{0.016 \text{ m}}}$$